

FINAL OPTICS MODELING

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OUTLINE

- Objectives of final optics modeling
- GIMM surface defect types and modeling approaches
- Fresnel modeling of multi-layer films
 - (1) Oxide-coated Al mirror
 - (2) Contaminated mirror
- Ray tracing and wave scattering approaches
- Future plans

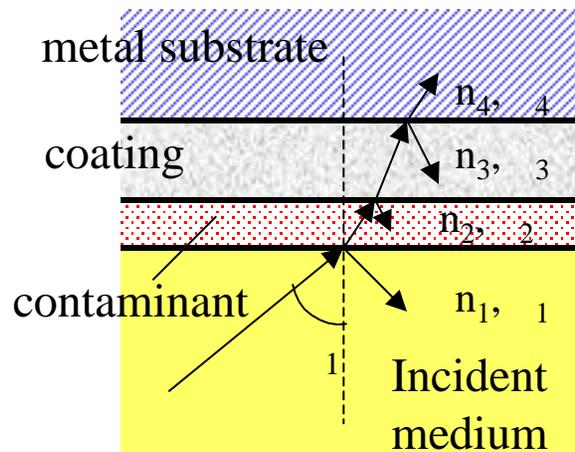
Modeling Objectives

- The GIMM (grazing incidence metal mirror) is subjected to damages from:
 - (1) X-rays, (2) γ -rays, (3) neutrons, (4) laser radiation, (5) charged particles, and (6) debris.
- The **primary objective** for final optics modeling is to quantitatively analyze the effects of these damages on the quality of laser beam focusing on the target.
A **secondary objective** is to more accurately define the design windows for the GIMM, such as power density threshold, protective coating, material selection, operational lifetime, than previously done.
- Damages to the mirror can have three main effects:
 - Beam (on target) defocusing, and wavefront distortion
 - Increased beam absorption at the mirror
 - Shorter mirror lifetime

Mirror Defects and Damage Types, and Approaches to Assess Beam Quality Degradation

Dimensional Defects		Compositional Defects	
Gross deformations, >	Surface morphology, <	Gross surface contamination	Local contamination
CONCERNS			
<ul style="list-style-type: none"> • Fabrication quality • Neutron swelling • Thermal swelling • Gravity loads 	<ul style="list-style-type: none"> • Laser-induced damage • Thermomechanical damage 	<ul style="list-style-type: none"> • Transmutations • Bulk redeposition 	<ul style="list-style-type: none"> • Aerosol, dust & debris
MODELLING TOOLS			
Optical design software	Potential scattering theory (perturbation analysis)	Fresnel equation solver	Potential scattering theory (perturbation analysis)

Fresnel Modeling of Reflectivity



- Wave propagation in four stratified layers of media is modeled. Surface is assumed to be smooth ($\lambda \gg \text{roughness}$). [Born & Wolf, Heavens]
- Each medium is homogeneous, with uniform thickness, and is characterized by complex refractive index: $n = n (1 + i \kappa)$
 $n = (\epsilon / \mu)^{1/2}$; $\kappa = \text{attenuation index}$
- TE (S) polarization is assumed.

- Refraction : $n_1 \sin \theta_1 = n_j \sin \theta_j \quad j = 2,3,4 \quad (\text{Snell's Law})$
- Reflection : $r_{i,i+1} = (n_i \cos \theta_i - n_{i+1} \cos \theta_{i+1}) / (n_i \cos \theta_i + n_{i+1} \cos \theta_{i+1}) \quad (\text{Fresnel})$
- Reflectivity is computed by repetitive usage of the 3-layer formula:

$$r_i = [r_{i-1,i} + r_{i+1} \exp (i2 \delta_i)] / [1 + r_{i-1,i} r_{i+1} \exp (i2 \delta_i)]$$

where $\delta_i = (2 \pi / \lambda_0) d_i n_i \cos \theta_i$, $i = 2,3$ and d_i is the layer thickness, and

setting intensity reflectivity as $R = |r_2|^2$.

S- and P- Polarizations

- Consider a plane EM wave propagating through a stratified medium with $\epsilon = \epsilon(z)$.

- Any arbitrarily polarized plane wave may be resolved into two waves:

(1) TE (S) with $E_s = E_x$, transverse to plane of incidence, i.e., y-z plane

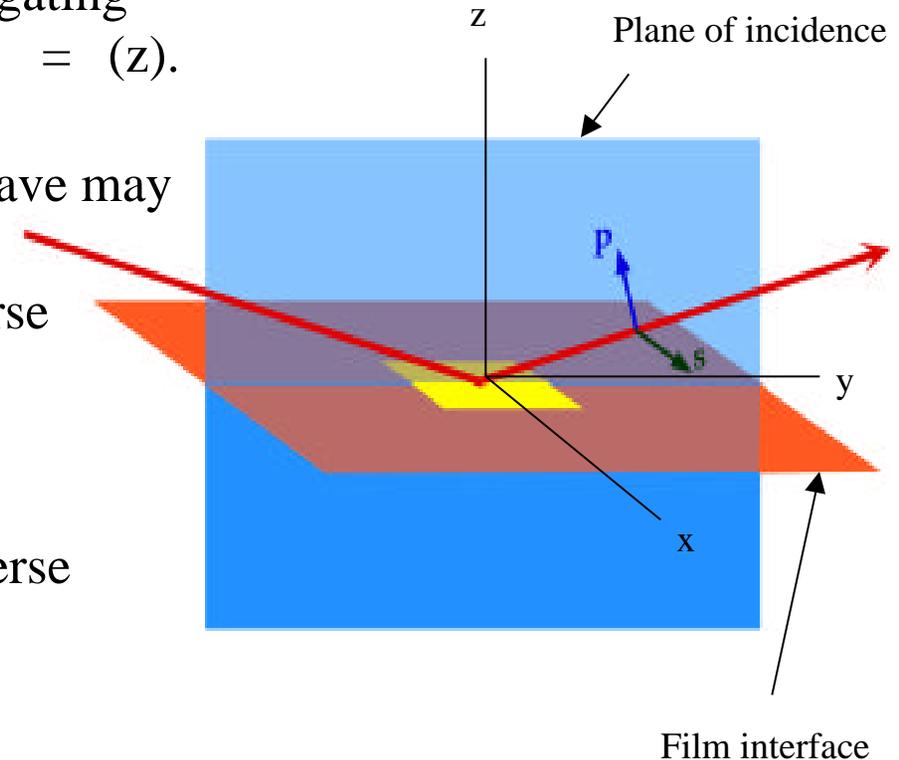
$$H = (H_y, H_z) = H_{\parallel} = H_s$$

(2) TM (P) with $H_p = H_x$, transverse to plane of incidence

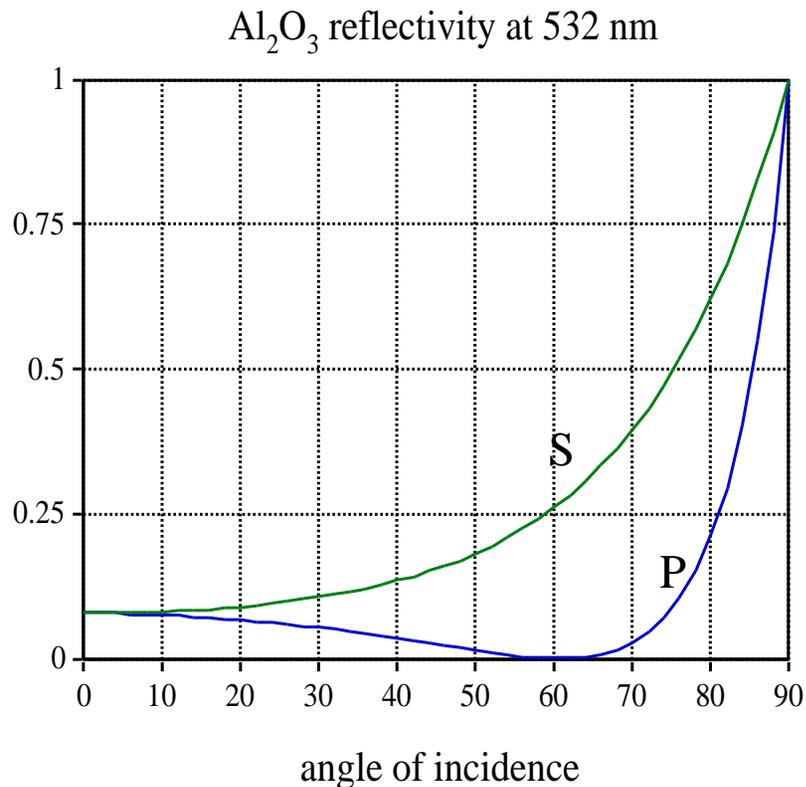
$$E = (E_y, E_z) = E_{\parallel} = E_p$$

- Thus, in vector form, $\underline{E}_{\text{tot}} = \underline{E}_s + \underline{E}_p$,

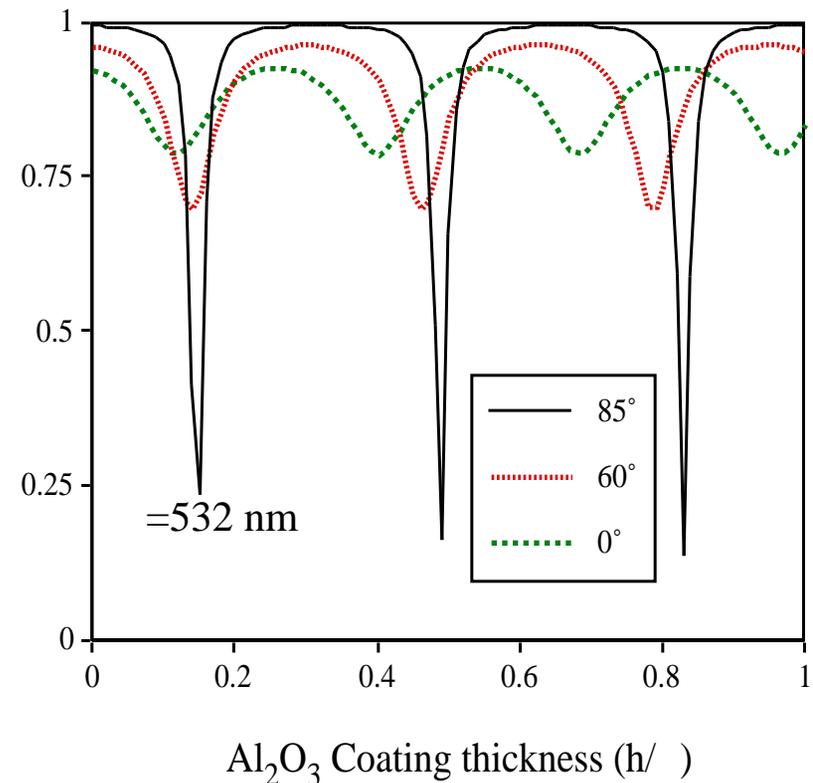
as shown in the diagram.



Reflection of S-polarized (TE) waves including thin oxide coating



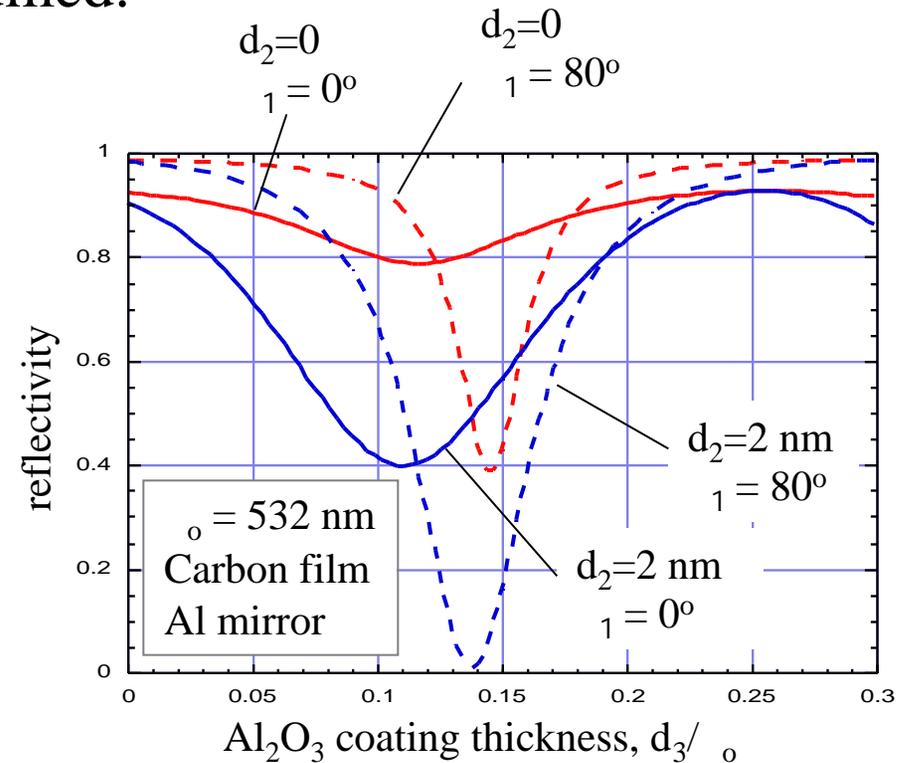
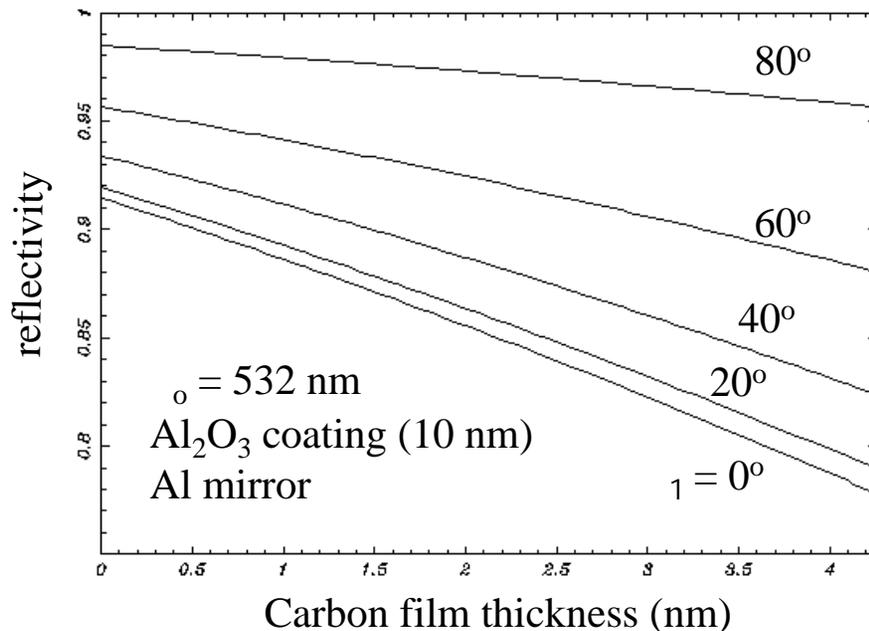
P-polarization undergoes total transmission at $\sim 60^\circ$.



Periodic variation in R is due to interference effect in oxide coating.

Effect of surface contaminants

- Surface contaminants (such as carbon) on mirror protective coatings can substantially alter reflectivity, depending on layer thickness and incident angle.
- Uniform film thickness is assumed.



Ray Tracing and Optical Design Software

- When surface defect $>$, effect on beam focusing can be assessed using the ray tracing approach.
- There are numerous optical design programs that perform ray tracing on all types of surfaces and media with complex refractive index.
- One such design package is ZEMAX-EE from Focus Software, Inc. Features include:
 - Complete polarization ray tracing and analysis capability (transmission, reflection, absorption, polarization state, etc)
 - Supports arbitrary user defined surfaces (shape, optical properties)
 - Extensive thin film modeling capability
 - Integrated tolerance analysis capability: RMS spot radius, RMS wavefront error, etc as criteria.
 - Nonlinear model of thermal effects on index of refraction and material expansion.
- Procurement of an optical design software package is being considered.

Wave Scattering from Rough Surfaces

- When surface roughness or deformation $\ll \lambda$, part of incident wave is scattered off the specular direction in a diffuse manner, thus degrading the focusing of the beam on a target.

- Two analysis approaches:

- **Perturbation theory** (Raleigh-Rice): valid for $\epsilon \ll 1$

Expand $\epsilon^{sc} = \epsilon_0^{sc} + \epsilon_1^{sc} + \epsilon_2^{sc} + \dots$ where $\epsilon_n^{sc} = \epsilon^{(n)}$

Surface roughness characterized by 2-D power spectral density:

$$P(\vec{k}) = \lim_{\Delta} \left\langle \frac{1}{\Delta} \left| \int_{\Delta} d\vec{r} e^{i\vec{k} \cdot \vec{r}} \zeta(\vec{r}) \right|^2 \right\rangle$$

- **Physical optics** (Kirchoff): valid for $\epsilon < 1$

Solve for total scattered field (coherent+diffuse), with approximation.

For Gaussian distribution, overall scattered intensity is given by

$\langle I \rangle = I_0 e^{-g} + \langle I_d \rangle$, where $g \ll 1$ for slightly rough surfaces, and $g \gg 1$ for very rough surfaces; I_0 is energy scattered from smooth surface, and I_d is diffuse intensity.

- Perturbation approach is simpler; physical optics technique is valid over wider range of surface roughness.

SUMMARY & FUTURE PLANS

- Fresnel analysis of oxide-coated metal mirrors has been carried out using a 4-layer model and assuming smooth surfaces.
 - Surface contaminant can have impact on reflectivity.
- Investigation into effects of mirror defects and induced damages on beam focusing has just begun.

Goal is to determine design windows for GIMM and other optical subsystems for ARIES/IFE studies by relating these damages to heat deposition and neutron fluence.
- Two approaches are being examined:
 - (1) Ray tracing with vendor design software (>)
ZEMAX-EE is a candidate package.
 - (2) Wave scattering approach (<)
Further study is required to identify appropriate method:
Perturbation analysis or physical optics?
 - * Examine if ZEMAX can be used for this purpose.
 - * Search for wave scattering software in public domain.